

165 Englands Lane

DESIGN PACK

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Project Brief:

Loft conversion.

Reference Documents:

- Architect Drawings

Design Codes:

- BSEN1990 Basis of structure
- BSEN1991 Actions on structure
- BSEN1992 Design of concrete structures
- BSEN1993 Design of steel structures
- BSEN1996 Design of masonry structures
- BSEN1995 Design of timber structures

Reference Design Software:

- TEDDS

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LOADS CALCULATIONS

TRIMMER T1

Timber Joists - Internal Floor Loads		
Item	Unfactored Load (KN/m²)	Load Type
Floor joists	0.15	Dead
Floor boards	0.05	Dead
Plaster board and Skim	0.25	Dead
Finish	0.05	Dead
Residential Live Loading	1.5	Live
TOTAL FLOOR DEAD LOAD	0.5 (KN/m²)	
TOTAL FLOOR LIVE LOAD	1.5 (KN/m²)	

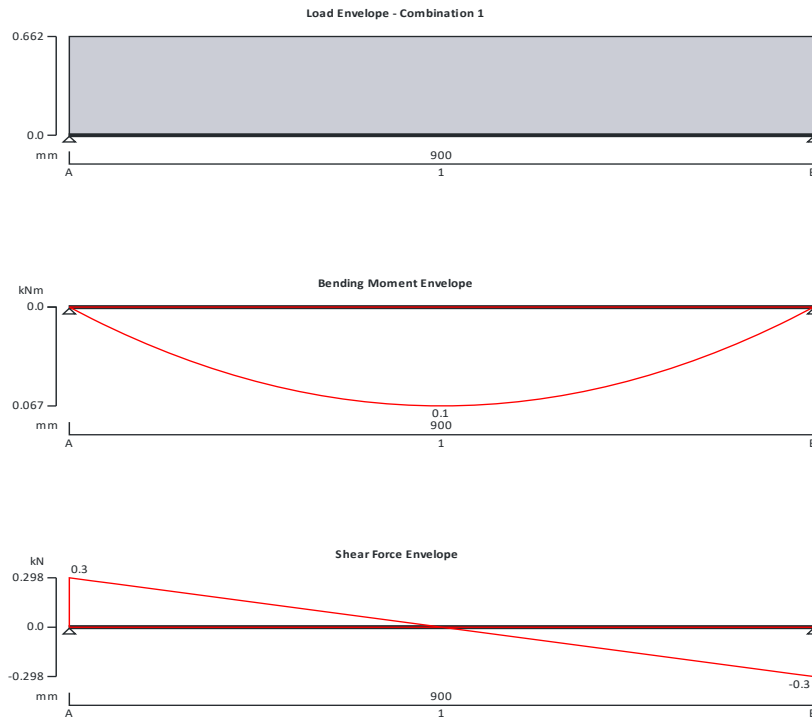
Proposed UDLs				
Item	Span (m)	Dead Load (KN/m²)	Live Load (KN/m²)	Comments
Loft Floor Loading	0.3	0.5	1.5	See Load Table For Internal Floor
		Total Dead	0.15 (KN/m)	
		Total Live	0.45 (KN/m)	

ANALYSIS & DESIGN

TRIMMER T1

TIMBER BEAM ANALYSIS & DESIGN TO BS5268-2:2002

TEDDS calculation version 1.7.03



Applied loading

Beam loads

Dead self weight of beam $\times 1$

Dead full UDL 0.150 kN/m

Imposed full UDL 0.450 kN/m

Load combinations

Load combination 1

Support A

Dead $\times 1.00$ Imposed $\times 1.00$

Span 1

Dead $\times 1.00$ Imposed $\times 1.00$

Support B

Dead $\times 1.00$ Imposed $\times 1.00$

Analysis results

Maximum moment

 $M_{\max} = 0.067$ kNm $M_{\min} = 0.000$ kNm

Design moment

 $M = \max(\text{abs}(M_{\max}), \text{abs}(M_{\min})) = 0.067$ kNm

Maximum shear

 $F_{\max} = 0.298$ kN $F_{\min} = -0.298$ kN

Design shear

 $F = \max(\text{abs}(F_{\max}), \text{abs}(F_{\min})) = 0.298$ kN

Total load on beam

 $W_{\text{tot}} = 0.596$ kN

Reactions at support A

 $R_{A_{\max}} = 0.298$ kN $R_{A_{\min}} = 0.298$ kN

Unfactored dead load reaction at support A

 $R_{A_{\text{Dead}}} = 0.095$ kN

ANALYSIS & DESIGN

TRIMMER T1

Unfactored imposed load reaction at support A

$$R_{A_Imposed} = 0.203 \text{ kN}$$

Reactions at support B

$$R_{B_max} = 0.298 \text{ kN}$$

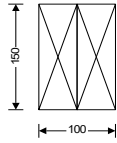
$$R_{B_min} = 0.298 \text{ kN}$$

Unfactored dead load reaction at support B

$$R_{B_Dead} = 0.095 \text{ kN}$$

Unfactored imposed load reaction at support B

$$R_{B_Imposed} = 0.203 \text{ kN}$$



Timber section details

Breadth of sections

$$b = 50 \text{ mm}$$

Depth of sections

$$h = 150 \text{ mm}$$

Number of sections in member

$$N = 2$$

Overall breadth of member

$$b_b = N \times b = 100 \text{ mm}$$

Timber strength class

C24

Member details

Service class of timber

1

Load duration

Long term

Length of span

$$L_{s1} = 900 \text{ mm}$$

Length of bearing

$$L_b = 100 \text{ mm}$$

Section properties

Cross sectional area of member

$$A = N \times b \times h = 15000 \text{ mm}^2$$

Section modulus

$$Z_x = N \times b \times h^2 / 6 = 375000 \text{ mm}^3$$

$$Z_y = h \times (N \times b)^2 / 6 = 250000 \text{ mm}^3$$

Second moment of area

$$I_x = N \times b \times h^3 / 12 = 28125000 \text{ mm}^4$$

$$I_y = h \times (N \times b)^3 / 12 = 12500000 \text{ mm}^4$$

Radius of gyration

$$i_x = \sqrt{I_x / A} = 43.3 \text{ mm}$$

$$i_y = \sqrt{I_y / A} = 28.9 \text{ mm}$$

Modification factors

Duration of loading - Table 17

$$K_3 = 1.00$$

Bearing stress - Table 18

$$K_4 = 1.00$$

Total depth of member - cl.2.10.6

$$K_7 = (300 \text{ mm} / h)^{0.11} = 1.08$$

Load sharing - cl.2.9

$$K_8 = 1.00$$

Lateral support - cl.2.10.8

No lateral support

Permissible depth-to-breadth ratio - Table 19

$$2.00$$

Actual depth-to-breadth ratio

$$h / (N \times b) = 1.50$$

PASS - Lateral support is adequate

Compression perpendicular to grain

Permissible bearing stress (no wane)

$$\sigma_{c_adm} = \sigma_{cp1} \times K_3 \times K_4 \times K_8 = 2.400 \text{ N/mm}^2$$

Applied bearing stress

$$\sigma_{c_a} = R_{A_max} / (N \times b \times L_b) = 0.030 \text{ N/mm}^2$$

$$\sigma_{c_a} / \sigma_{c_adm} = 0.012$$

PASS - Applied compressive stress is less than permissible compressive stress at bearing

ANALYSIS & DESIGN

TRIMMER T1

Bending parallel to grain

Permissible bending stress

$$\sigma_{m_adm} = \sigma_m \times K_3 \times K_7 \times K_8 = \mathbf{8.094 \text{ N/mm}^2}$$

Applied bending stress

$$\sigma_{m_a} = M / Z_x = \mathbf{0.179 \text{ N/mm}^2}$$

$$\sigma_{m_a} / \sigma_{m_adm} = \mathbf{0.022}$$

PASS - Applied bending stress is less than permissible bending stress**Shear parallel to grain**

Permissible shear stress

$$\tau_{adm} = \tau \times K_3 \times K_8 = \mathbf{0.710 \text{ N/mm}^2}$$

Applied shear stress

$$\tau_a = 3 \times F / (2 \times A) = \mathbf{0.030 \text{ N/mm}^2}$$

$$\tau_a / \tau_{adm} = \mathbf{0.042}$$

PASS - Applied shear stress is less than permissible shear stress**Deflection**

Modulus of elasticity for deflection

$$E = E_{min} = \mathbf{7200 \text{ N/mm}^2}$$

Permissible deflection

$$\delta_{adm} = \min(0.551 \text{ in}, 0.003 \times L_{s1}) = \mathbf{2.700 \text{ mm}}$$

Bending deflection

$$\delta_{b_s1} = \mathbf{0.028 \text{ mm}}$$

Shear deflection

$$\delta_{v_s1} = \mathbf{0.012 \text{ mm}}$$

Total deflection

$$\delta_a = \delta_{b_s1} + \delta_{v_s1} = \mathbf{0.040 \text{ mm}}$$

$$\delta_a / \delta_{adm} = \mathbf{0.015}$$

PASS - Total deflection is less than permissible deflection

LOADS CALCULATIONS
TRIMMER T2

Timber Joists - Internal Floor Loads		
Item	Unfactored Load (KN/m²)	Load Type
Floor joists	0.15	Dead
Floor boards	0.05	Dead
Plaster board and Skim	0.25	Dead
Finish	0.05	Dead
Residential Live Loading	1.5	Live
TOTAL FLOOR DEAD LOAD		0.5 (KN/m²)
TOTAL FLOOR LIVE LOAD		1.5 (KN/m²)

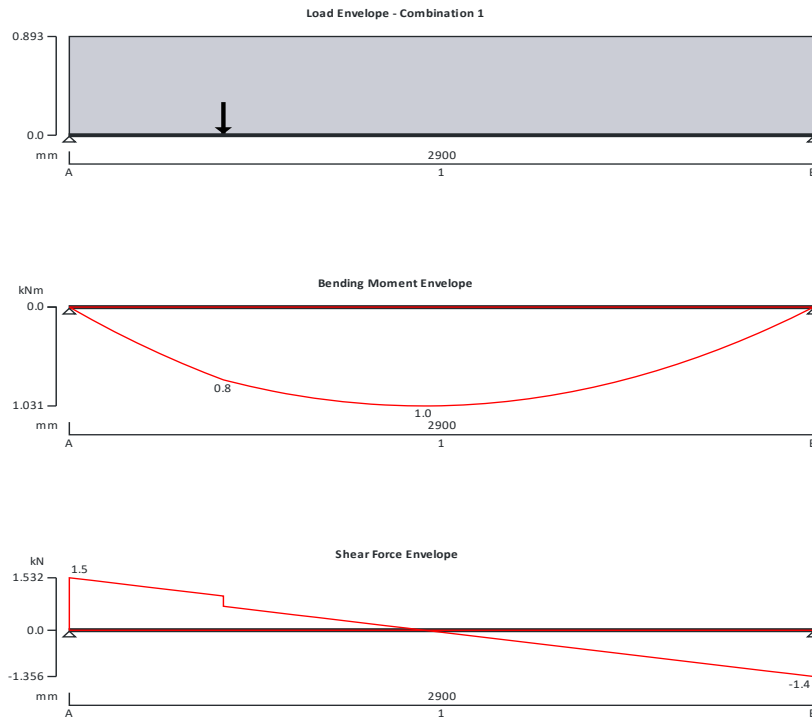
Proposed UDLs				
Item	Span (m)	Dead Load (KN/m²)	Live Load (KN/m²)	Comments
Loft Floor Loading	0.4	0.5	1.5	See Load Table For Internal Floor
T1 Reaction	-	-	-	0.3 KN @ 600mm
		Total Dead	0.2 (KN/m)	
		Total Live	0.6 (KN/m)	

ANALYSIS & DESIGN

TRIMMER T2

TIMBER BEAM ANALYSIS & DESIGN TO BS5268-2:2002

TEDDS calculation version 1.7.03



Applied loading

Beam loads

Dead self weight of beam $\times 1$
 Dead full UDL 0.200 kN/m
 Imposed full UDL 0.600 kN/m
 Other point load 0.300 kN at 600 mm

Load combinations

Load combination 1

Support A

Dead $\times 1.00$
 Imposed $\times 1.00$
 Other $\times 1.00$

Span 1

Dead $\times 1.00$
 Imposed $\times 1.00$
 Other $\times 1.00$

Support B

Dead $\times 1.00$
 Imposed $\times 1.00$
 Other $\times 1.00$

Analysis results

Maximum moment

 $M_{\max} = 1.031$ kNm $M_{\min} = 0.000$ kNm

Design moment

 $M = \max(\text{abs}(M_{\max}), \text{abs}(M_{\min})) = 1.031$ kNm

Maximum shear

 $F_{\max} = 1.532$ kN $F_{\min} = -1.356$ kN

ANALYSIS & DESIGN

TRIMMER T2

Design shear

Total load on beam

Reactions at support A

Unfactored dead load reaction at support A

Unfactored imposed load reaction at support A

Unfactored other load reaction at support A

Reactions at support B

Unfactored dead load reaction at support B

Unfactored imposed load reaction at support B

Unfactored other load reaction at support B

$$F = \max(\text{abs}(F_{\max}), \text{abs}(F_{\min})) = 1.532 \text{ kN}$$

$$W_{\text{tot}} = 2.889 \text{ kN}$$

$$R_{A_{\max}} = 1.532 \text{ kN}$$

$$R_{A_{\min}} = 1.532 \text{ kN}$$

$$R_{A_{\text{Dead}}} = 0.424 \text{ kN}$$

$$R_{A_{\text{Imposed}}} = 0.870 \text{ kN}$$

$$R_{A_{\text{Other}}} = 0.238 \text{ kN}$$

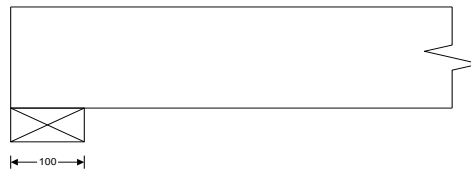
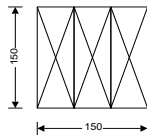
$$R_{B_{\max}} = 1.356 \text{ kN}$$

$$R_{B_{\min}} = 1.356 \text{ kN}$$

$$R_{B_{\text{Dead}}} = 0.424 \text{ kN}$$

$$R_{B_{\text{Imposed}}} = 0.870 \text{ kN}$$

$$R_{B_{\text{Other}}} = 0.062 \text{ kN}$$



Timber section details

Breadth of sections

$$b = 50 \text{ mm}$$

Depth of sections

$$h = 150 \text{ mm}$$

Number of sections in member

$$N = 3$$

Overall breadth of member

$$b_b = N \times b = 150 \text{ mm}$$

Timber strength class

C24

Member details

Service class of timber

1

Load duration

Long term

Length of span

$$L_{s1} = 2900 \text{ mm}$$

Length of bearing

$$L_b = 100 \text{ mm}$$

Section properties

Cross sectional area of member

$$A = N \times b \times h = 22500 \text{ mm}^2$$

Section modulus

$$Z_x = N \times b \times h^2 / 6 = 562500 \text{ mm}^3$$

$$Z_y = h \times (N \times b)^2 / 6 = 562500 \text{ mm}^3$$

Second moment of area

$$I_x = N \times b \times h^3 / 12 = 42187500 \text{ mm}^4$$

$$I_y = h \times (N \times b)^3 / 12 = 42187500 \text{ mm}^4$$

Radius of gyration

$$i_x = \sqrt{I_x / A} = 43.3 \text{ mm}$$

$$i_y = \sqrt{I_y / A} = 43.3 \text{ mm}$$

Modification factors

Duration of loading - Table 17

$$K_3 = 1.00$$

Bearing stress - Table 18

$$K_4 = 1.00$$

Total depth of member - cl.2.10.6

$$K_7 = (300 \text{ mm} / h)^{0.11} = 1.08$$

Load sharing - cl.2.9

$$K_8 = 1.00$$

Lateral support - cl.2.10.8

No lateral support

$$2.00$$

Permissible depth-to-breadth ratio - Table 19

$$h / (N \times b) = 1.00$$

Actual depth-to-breadth ratio

PASS - Lateral support is adequate

ANALYSIS & DESIGN

TRIMMER T2

Compression perpendicular to grain

Permissible bearing stress (no wane)

$$\sigma_{c_adm} = \sigma_{cp1} \times K_3 \times K_4 \times K_8 = \mathbf{2.400 \text{ N/mm}^2}$$

Applied bearing stress

$$\sigma_{c_a} = R_{A_max} / (N \times b \times L_b) = \mathbf{0.102 \text{ N/mm}^2}$$

$$\sigma_{c_a} / \sigma_{c_adm} = \mathbf{0.043}$$

PASS - Applied compressive stress is less than permissible compressive stress at bearing

Bending parallel to grain

Permissible bending stress

$$\sigma_{m_adm} = \sigma_m \times K_3 \times K_7 \times K_8 = \mathbf{8.094 \text{ N/mm}^2}$$

Applied bending stress

$$\sigma_{m_a} = M / Z_x = \mathbf{1.832 \text{ N/mm}^2}$$

$$\sigma_{m_a} / \sigma_{m_adm} = \mathbf{0.226}$$

PASS - Applied bending stress is less than permissible bending stress

Shear parallel to grain

Permissible shear stress

$$\tau_{adm} = \tau \times K_3 \times K_8 = \mathbf{0.710 \text{ N/mm}^2}$$

Applied shear stress

$$\tau_a = 3 \times F / (2 \times A) = \mathbf{0.102 \text{ N/mm}^2}$$

$$\tau_a / \tau_{adm} = \mathbf{0.144}$$

PASS - Applied shear stress is less than permissible shear stress

Deflection

Modulus of elasticity for deflection

$$E = E_{min} = \mathbf{7200 \text{ N/mm}^2}$$

Permissible deflection

$$\delta_{adm} = \min(0.551 \text{ in}, 0.003 \times L_{s1}) = \mathbf{8.700 \text{ mm}}$$

Bending deflection

$$\delta_{b_s1} = \mathbf{3.006 \text{ mm}}$$

Shear deflection

$$\delta_{v_s1} = \mathbf{0.128 \text{ mm}}$$

Total deflection

$$\delta_a = \delta_{b_s1} + \delta_{v_s1} = \mathbf{3.134 \text{ mm}}$$

$$\delta_a / \delta_{adm} = \mathbf{0.360}$$

PASS - Total deflection is less than permissible deflection

ANALYSIS & DESIGN

LOFT FLOOR JOISTS

TIMBER JOIST DESIGN (BS5268-2:2002)

Teds calculation version 1.1.04

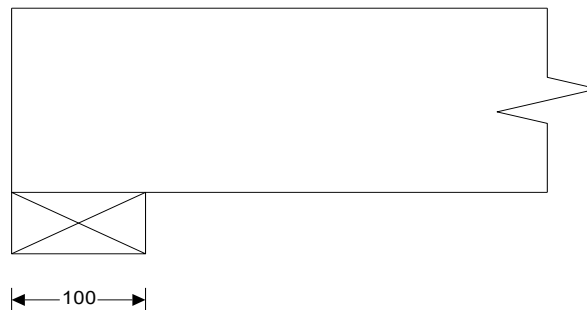
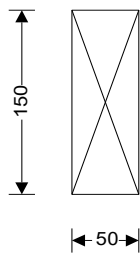
Joist details

Joist breadth	$b = 50 \text{ mm}$
Joist depth	$h = 150 \text{ mm}$
Joist spacing	$s = 400 \text{ mm}$
Timber strength class	C24
Service class of timber	1



Span details

Number of spans	$N_{\text{span}} = 1$
Length of bearing	$L_b = 100 \text{ mm}$
Effective length of span	$L_{s1} = 2900 \text{ mm}$



Section properties

Second moment of area	$I = b \times h^3 / 12 = 14062500 \text{ mm}^4$
Section modulus	$Z = b \times h^2 / 6 = 187500 \text{ mm}^3$

Loading details

Joist self weight	$F_{\text{swt}} = b \times h \times \rho_{\text{char}} \times g_{\text{acc}} = 0.03 \text{ kN/m}$
Dead load	$F_{\text{d_udl}} = 0.50 \text{ kN/m}^2$
Imposed UDL(Long term)	$F_{\text{i_udl}} = 1.50 \text{ kN/m}^2$
Imposed point load (Medium term)	$F_{\text{i_pt}} = 1.40 \text{ kN}$

Modification factors

Service class for bending parallel to grain	$K_{2m} = 1.00$
Service class for compression	$K_{2c} = 1.00$
Service class for shear parallel to grain	$K_{2s} = 1.00$
Service class for modulus of elasticity	$K_{2e} = 1.00$
Section depth factor	$K_7 = 1.08$
Load sharing factor	$K_8 = 1.10$

ANALYSIS & DESIGN

LOFT FLOOR JOISTS

Consider long term loads

Load duration factor	$K_3 = 1.00$
Maximum bending moment	$M = 0.868 \text{ kNm}$
Maximum shear force	$V = 1.197 \text{ kN}$
Maximum support reaction	$R = 1.197 \text{ kN}$
Maximum deflection	$\delta = 5.213 \text{ mm}$

Check bending stress

Bending stress	$\sigma_m = 7.500 \text{ N/mm}^2$
Permissible bending stress	$\sigma_{m_adm} = \sigma_m \times K_{2s} \times K_3 \times K_7 \times K_8 = 8.904 \text{ N/mm}^2$
Applied bending stress	$\sigma_{m_max} = M / Z = 4.630 \text{ N/mm}^2$

PASS - Applied bending stress within permissible limits

Check shear stress

Shear stress	$\tau = 0.710 \text{ N/mm}^2$
Permissible shear stress	$\tau_{adm} = \tau \times K_{2s} \times K_3 \times K_8 = 0.781 \text{ N/mm}^2$
Applied shear stress	$\tau_{max} = 3 \times V / (2 \times b \times h) = 0.239 \text{ N/mm}^2$

PASS - Applied shear stress within permissible limits

Check bearing stress

Compression perpendicular to grain (no wane)	$\sigma_{cp1} = 2.400 \text{ N/mm}^2$
Permissible bearing stress	$\sigma_{c_adm} = \sigma_{cp1} \times K_{2c} \times K_3 \times K_8 = 2.640 \text{ N/mm}^2$
Applied bearing stress	$\sigma_{c_max} = R / (b \times L_b) = 0.239 \text{ N/mm}^2$

PASS - Applied bearing stress within permissible limits

Check deflection

Permissible deflection	$\delta_{adm} = \min(L_{s1} \times 0.003, 14 \text{ mm}) = 8.700 \text{ mm}$
Bending deflection (based on E_{mean})	$\delta_{bending} = 5.007 \text{ mm}$
Shear deflection	$\delta_{shear} = 0.206 \text{ mm}$
Total deflection	$\delta = \delta_{bending} + \delta_{shear} = 5.213 \text{ mm}$

PASS - Actual deflection within permissible limits

Consider medium term loads

Load duration factor	$K_3 = 1.25$
Maximum bending moment	$M = 1.252 \text{ kNm}$
Maximum shear force	$V = 1.727 \text{ kN}$
Maximum support reaction	$R = 1.727 \text{ kN}$
Maximum deflection	$\delta = 6.349 \text{ mm}$

Check bending stress

Bending stress	$\sigma_m = 7.500 \text{ N/mm}^2$
Permissible bending stress	$\sigma_{m_adm} = \sigma_m \times K_{2m} \times K_3 \times K_7 \times K_8 = 11.130 \text{ N/mm}^2$
Applied bending stress	$\sigma_{m_max} = M / Z = 6.679 \text{ N/mm}^2$

PASS - Applied bending stress within permissible limits

Check shear stress

Shear stress	$\tau = 0.710 \text{ N/mm}^2$
Permissible shear stress	$\tau_{adm} = \tau \times K_{2s} \times K_3 \times K_8 = 0.976 \text{ N/mm}^2$
Applied shear stress	$\tau_{max} = 3 \times V / (2 \times b \times h) = 0.345 \text{ N/mm}^2$

PASS - Applied shear stress within permissible limits

ANALYSIS & DESIGN

LOFT FLOOR JOISTS

Check bearing stress

Compression perpendicular to grain (no wane)

$$\sigma_{cp1} = \mathbf{2.400 \text{ N/mm}^2}$$

Permissible bearing stress

$$\sigma_{c_adm} = \sigma_{cp1} \times K_{2c} \times K_3 \times K_8 = \mathbf{3.300 \text{ N/mm}^2}$$

Applied bearing stress

$$\sigma_{c_max} = R / (b \times L_b) = \mathbf{0.345 \text{ N/mm}^2}$$

PASS - Applied bearing stress within permissible limits

Check deflection

Permissible deflection

$$\delta_{adm} = \min(L_{s1} \times 0.003, 14 \text{ mm}) = \mathbf{8.700 \text{ mm}}$$

Bending deflection (based on E_{mean})

$$\delta_{bending} = \mathbf{6.053 \text{ mm}}$$

Shear deflection

$$\delta_{shear} = \mathbf{0.297 \text{ mm}}$$

Total deflection

$$\delta = \delta_{bending} + \delta_{shear} = \mathbf{6.349 \text{ mm}}$$

PASS - Actual deflection within permissible limits

ANALYSIS & DESIGN

FLAT ROOF JOISTS

TIMBER JOIST DESIGN (BS5268-2:2002)

Teds calculation version 1.1.04

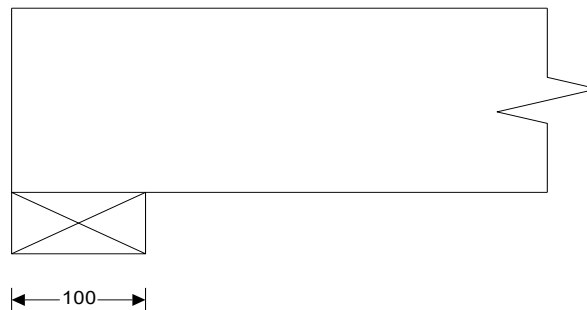
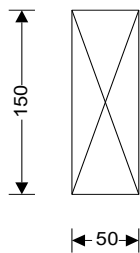
Joist details

Joist breadth	$b = 50 \text{ mm}$
Joist depth	$h = 150 \text{ mm}$
Joist spacing	$s = 400 \text{ mm}$
Timber strength class	C24
Service class of timber	1



Span details

Number of spans	$N_{\text{span}} = 1$
Length of bearing	$L_b = 100 \text{ mm}$
Effective length of span	$L_{s1} = 3300 \text{ mm}$



Section properties

Second moment of area	$I = b \times h^3 / 12 = 14062500 \text{ mm}^4$
Section modulus	$Z = b \times h^2 / 6 = 187500 \text{ mm}^3$

Loading details

Joist self weight	$F_{\text{swt}} = b \times h \times \rho_{\text{char}} \times g_{\text{acc}} = 0.03 \text{ kN/m}$
Dead load	$F_{\text{d_udl}} = 0.85 \text{ kN/m}^2$
Imposed UDL(Medium term)	$F_{\text{i_udl}} = 0.75 \text{ kN/m}^2$
Imposed point load (Short term)	$F_{\text{i_pt}} = 0.90 \text{ kN}$

Modification factors

Service class for bending parallel to grain	$K_{2m} = 1.00$
Service class for compression	$K_{2c} = 1.00$
Service class for shear parallel to grain	$K_{2s} = 1.00$
Service class for modulus of elasticity	$K_{2e} = 1.00$
Section depth factor	$K_7 = 1.08$
Load sharing factor	$K_8 = 1.10$

ANALYSIS & DESIGN

FLAT ROOF JOISTS

Consider medium term loads

Load duration factor	$K_3 = 1.25$
Maximum bending moment	$M = 0.906 \text{ kNm}$
Maximum shear force	$V = 1.098 \text{ kN}$
Maximum support reaction	$R = 1.098 \text{ kN}$
Maximum deflection	$\delta = 6.984 \text{ mm}$

Check bending stress

Bending stress	$\sigma_m = 7.500 \text{ N/mm}^2$
Permissible bending stress	$\sigma_{m_adm} = \sigma_m \times K_{2s} \times K_3 \times K_7 \times K_8 = 11.130 \text{ N/mm}^2$
Applied bending stress	$\sigma_{m_max} = M / Z = 4.833 \text{ N/mm}^2$

PASS - Applied bending stress within permissible limits

Check shear stress

Shear stress	$\tau = 0.710 \text{ N/mm}^2$
Permissible shear stress	$\tau_{adm} = \tau \times K_{2s} \times K_3 \times K_8 = 0.976 \text{ N/mm}^2$
Applied shear stress	$\tau_{max} = 3 \times V / (2 \times b \times h) = 0.220 \text{ N/mm}^2$

PASS - Applied shear stress within permissible limits

Check bearing stress

Compression perpendicular to grain (no wane)	$\sigma_{cp1} = 2.400 \text{ N/mm}^2$
Permissible bearing stress	$\sigma_{c_adm} = \sigma_{cp1} \times K_{2c} \times K_3 \times K_8 = 3.300 \text{ N/mm}^2$
Applied bearing stress	$\sigma_{c_max} = R / (b \times L_b) = 0.220 \text{ N/mm}^2$

PASS - Applied bearing stress within permissible limits

Check deflection

Permissible deflection	$\delta_{adm} = \min(L_{s1} \times 0.003, 14 \text{ mm}) = 9.900 \text{ mm}$
Bending deflection (based on E_{mean})	$\delta_{bending} = 6.769 \text{ mm}$
Shear deflection	$\delta_{shear} = 0.215 \text{ mm}$
Total deflection	$\delta = \delta_{bending} + \delta_{shear} = 6.984 \text{ mm}$

PASS - Actual deflection within permissible limits

Consider short term loads

Load duration factor	$K_3 = 1.50$
Maximum bending moment	$M = 1.240 \text{ kNm}$
Maximum shear force	$V = 1.503 \text{ kN}$
Maximum support reaction	$R = 1.503 \text{ kN}$
Maximum deflection	$\delta = 8.449 \text{ mm}$

Check bending stress

Bending stress	$\sigma_m = 7.500 \text{ N/mm}^2$
Permissible bending stress	$\sigma_{m_adm} = \sigma_m \times K_{2m} \times K_3 \times K_7 \times K_8 = 13.355 \text{ N/mm}^2$
Applied bending stress	$\sigma_{m_max} = M / Z = 6.615 \text{ N/mm}^2$

PASS - Applied bending stress within permissible limits

Check shear stress

Shear stress	$\tau = 0.710 \text{ N/mm}^2$
Permissible shear stress	$\tau_{adm} = \tau \times K_{2s} \times K_3 \times K_8 = 1.172 \text{ N/mm}^2$
Applied shear stress	$\tau_{max} = 3 \times V / (2 \times b \times h) = 0.301 \text{ N/mm}^2$

PASS - Applied shear stress within permissible limits

ANALYSIS & DESIGN

FLAT ROOF JOISTS

Check bearing stress

Compression perpendicular to grain (no wane)

$$\sigma_{cp1} = \mathbf{2.400 \text{ N/mm}^2}$$

Permissible bearing stress

$$\sigma_{c_adm} = \sigma_{cp1} \times K_{2c} \times K_3 \times K_8 = \mathbf{3.960 \text{ N/mm}^2}$$

Applied bearing stress

$$\sigma_{c_max} = R / (b \times L_b) = \mathbf{0.301 \text{ N/mm}^2}$$

PASS - Applied bearing stress within permissible limits**Check deflection**

Permissible deflection

$$\delta_{adm} = \min(L_{s1} \times 0.003, 14 \text{ mm}) = \mathbf{9.900 \text{ mm}}$$

Bending deflection (based on E_{mean})

$$\delta_{bending} = \mathbf{8.155 \text{ mm}}$$

Shear deflection

$$\delta_{shear} = \mathbf{0.294 \text{ mm}}$$

Total deflection

$$\delta = \delta_{bending} + \delta_{shear} = \mathbf{8.449 \text{ mm}}$$

PASS - Actual deflection within permissible limits

ANALYSIS & DESIGN

PITCHED ROOF RAFTERS

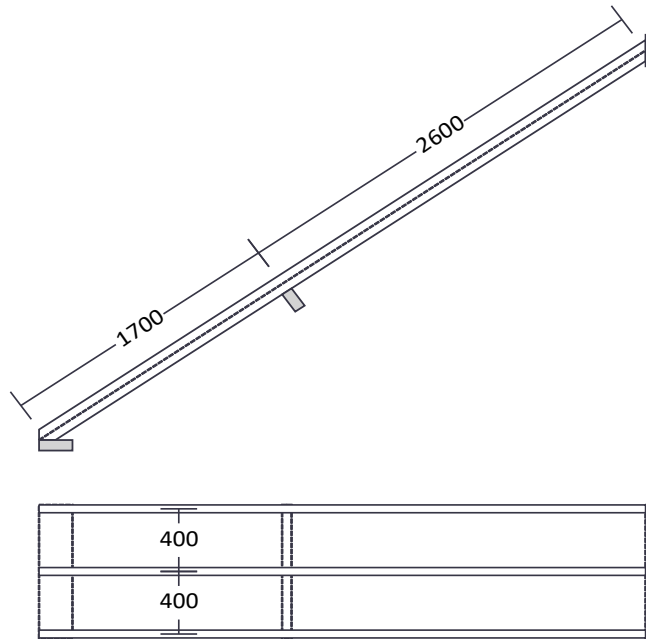
TIMBER RAFTER ANALYSIS & DESIGN (EN1995-1-1:2004)

In accordance with EN1995-1-1:2004 + A2:2014 incorporating corrigendum June 2006 and the UK national annex

Tedds calculation version 1.0.09

Rafter details

Description	50 x 110 C16 timber rafters
Rafter spacing	$s_{\text{Rafter}} = 400 \text{ mm}$
Rafter inclination	$\theta_{\text{Rafter}} = 35 \text{ deg}$



Forces input on Rafter

Permanent load on slope	$F_{G_Rafter} = 1.18 \text{ kN/m}^2$
Imposed load on plan	$F_{Q_Rafter} = 0.50 \text{ kN/m}^2$

Rafter loading details

Distributed loads

Permanent load on slope	$p_G = F_{G_Rafter} \times s_{\text{Rafter}} = 0.47 \text{ kN/m}$
Imposed load on slope	$p_Q = F_{Q_Rafter} \times s_{\text{Rafter}} \times \cos(\theta_{\text{Rafter}}) = 0.16 \text{ kN/m}$

Member span 1 results summary	Unit	Capacity	Maximum	Utilisation	Result
Compressive stress	N/mm ²	11.5	0.4	0.035	PASS
Bearing stress	N/mm ²	1.5	0.3	0.229	PASS
Bending stress	N/mm ²	11.5	4.7	0.412	PASS
Shear stress	N/mm ²	2.2	0.4	0.171	PASS
Bending and axial force				0.413	PASS
Column stability check				0.457	PASS
Beam stability check				0.203	PASS
Deflection	mm	6.8	0.4	0.065	PASS

ANALYSIS & DESIGN

PITCHED ROOF RAFTERS

Member span 2 results summary	Unit	Capacity	Maximum	Utilisation	Result
Compressive stress	N/mm ²	11.5	0.2	0.021	PASS
Bearing stress	N/mm ²	1.5	0.3	0.173	PASS
Bending stress	N/mm ²	11.5	4.7	0.412	PASS
Shear stress	N/mm ²	2.2	0.5	0.216	PASS
Bending and axial force				0.412	PASS
Column stability check				0.457	PASS
Beam stability check				0.190	PASS
Deflection	mm	10.4	7.4	0.716	PASS

ANALYSIS

Teds calculation version 1.0.38

Loading

Self weight included (Permanent x 1)

Load combination factors

Load combination	Permanent	Imposed	Snow	Wind
1.35G + 1.50Q (Strength)	1.35	1.50	0.00	0.00
1.00G + 1.00Q (Service)	1.00	1.00	0.00	0.00

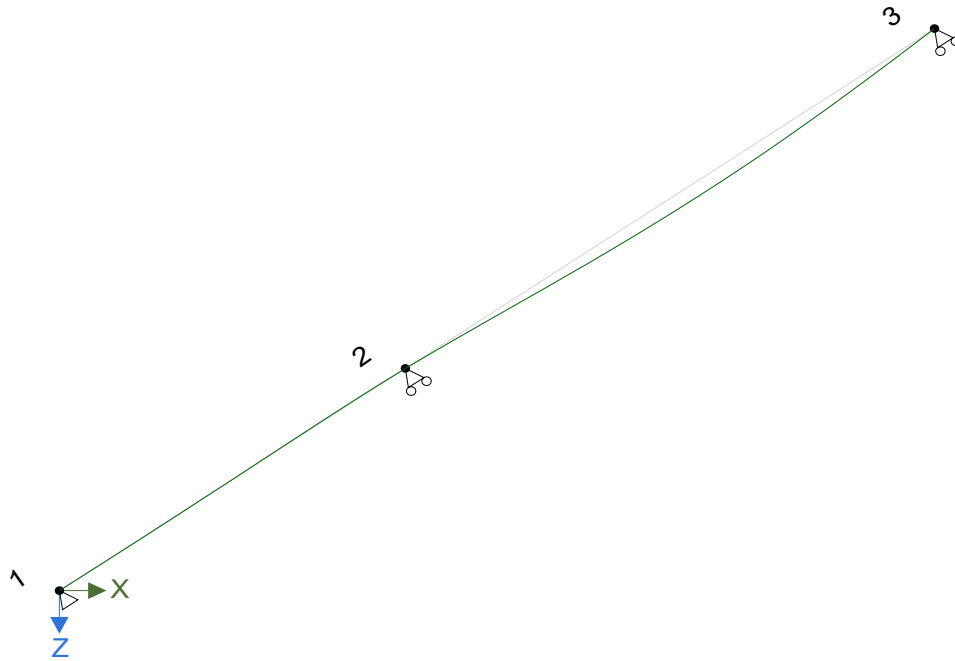
Member Loads

Member	Load case	Load Type	Orientation	Description
Member	Permanent	UDL	GlobalZ	0.47 kN/m at 0 m to 4.3 m
Member	Imposed	UDL	GlobalZ	0.16 kN/m at 0 m to 4.3 m

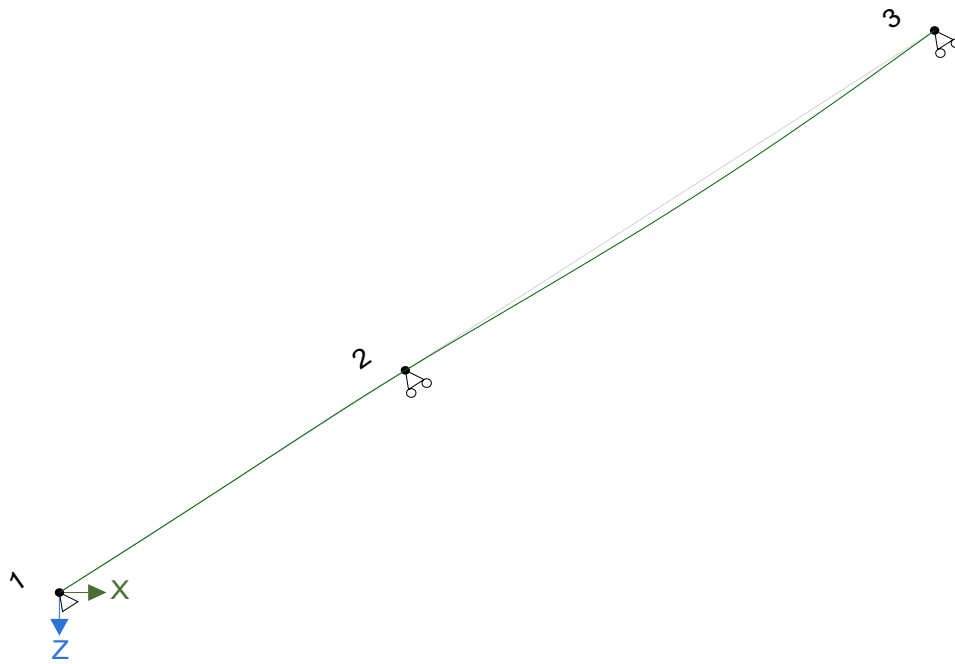
Results

Total deflection

1.35G + 1.50Q (Strength) - Total deflection



1.00G + 1.00Q (Service) - Total deflection



ANALYSIS & DESIGN

PITCHED ROOF RAFTERS

Node deflections

Load combination: 1.35G + 1.50Q (Strength)

Node	Deflection		Rotation (°)	Co-ordinate system
	X (mm)	Z (mm)		
1	0	0	0.028	Member
2	-0.1	0	0.16121	Member
3	-0.1	0	-0.43827	Member

Load combination: 1.00G + 1.00Q (Service)

Node	Deflection		Rotation (°)	Co-ordinate system
	X (mm)	Z (mm)		
1	0	0	0.02018	Member
2	0	0	0.11617	Member
3	-0.1	0	-0.31583	Member

Total base reactions

Load case/combination	Force	
	FX (kN)	FZ (kN)
1.35G + 1.50Q (Strength)	0	3.9
1.00G + 1.00Q (Service)	0	2.8

Element end forces

Load combination: 1.35G + 1.50Q (Strength)

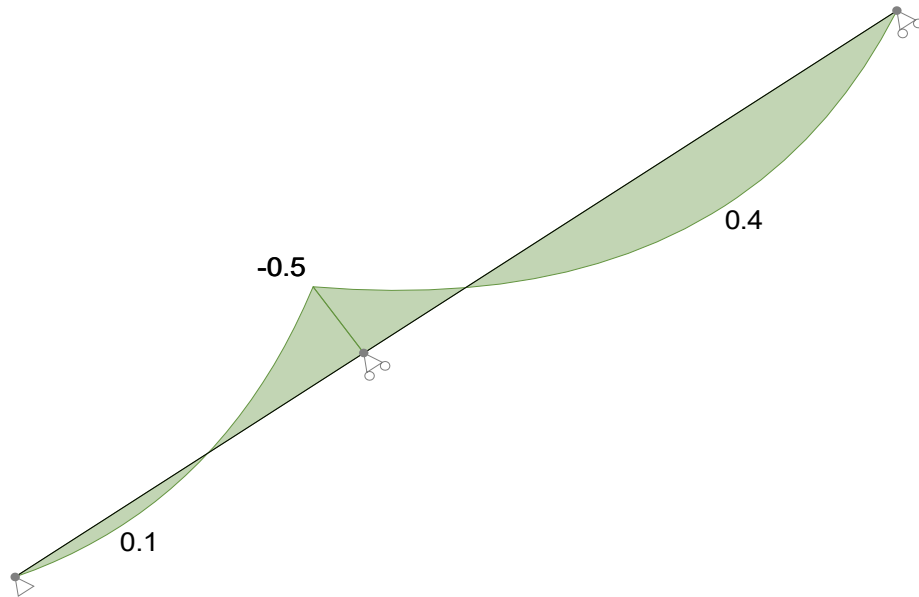
Element	Length (m)	Nodes Start/End	Axial force (kN)	Shear force (kN)	Moment (kNm)
1	1.7	1	-2.2	-0.3	0
		2	1.4	-0.9	-0.5
2	2.6	2	-1.4	-1.1	0.5
		3	0	-0.8	0

Load combination: 1.00G + 1.00Q (Service)

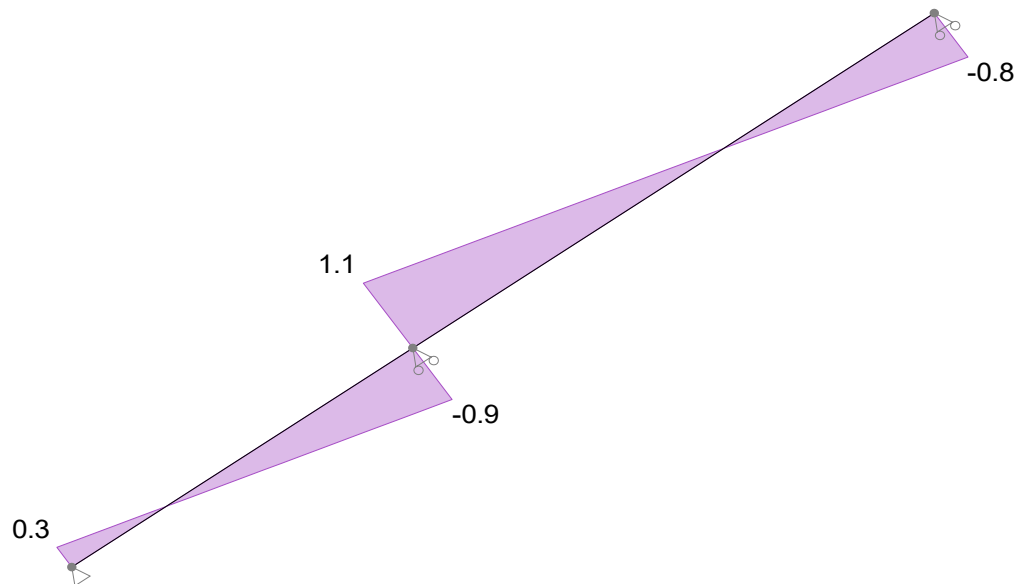
Element	Length (m)	Nodes Start/End	Axial force (kN)	Shear force (kN)	Moment (kNm)
1	1.7	1	-1.6	-0.3	0
		2	1	-0.7	-0.3
2	2.6	2	-1	-0.8	0.3
		3	0	-0.6	0

Forces

Strength combinations - Moment envelope (kNm)



Strength combinations - Shear envelope (kN)



ANALYSIS & DESIGN

PITCHED ROOF RAFTERS

Member results

Envelope - Strength combinations

Member	Position (m)	Shear force (kN)		Moment (kNm)	
Member	1.7	1.1 (max abs)	-0.9	-0.5 (min)	
	3.248	0		0.4 (max)	

Teds calculation version 2.2.23

Member - Span 1

Partial factor for material properties and resistances

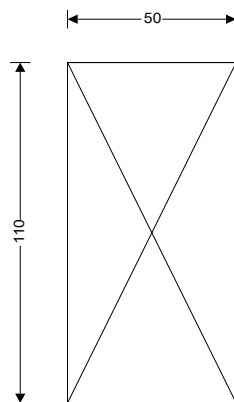
Partial factor for material properties - Table 2.3 $\gamma_M = 1.300$

Member details

Load duration - cl.2.3.1.2 Medium-term

Service class - cl.2.3.1.3 2

Timber section details

Number of timber sections in member $N = 1$ Breadth of sections $b = 50$ mmDepth of sections $h = 110$ mmTimber strength class - EN 338:2016 Table 1 **C16**

50x110 timber section

Cross-sectional area, A , 5500 mm²Section modulus, W_y , 100833.3 mm³Section modulus, W_z , 45833 mm³Second moment of area, I_y , 5545833 mm⁴Second moment of area, I_z , 1145833 mm⁴Radius of gyration, i_y , 31.8 mmRadius of gyration, i_z , 14.4 mm

Timber strength class C16

Characteristic bending strength, $f_{b,k}$, 16 N/mm²Characteristic shear strength, $f_{v,k}$, 3.2 N/mm²Characteristic compression strength parallel to grain, $f_{c,0,k}$, 17 N/mm²Characteristic compression strength perpendicular to grain, $f_{c,90,k}$, 2.2 N/mm²Characteristic tension strength parallel to grain, $f_{t,0,k}$, 8.5 N/mm²Mean modulus of elasticity, $E_{0,mean}$, 8000 N/mm²Fifth percentile modulus of elasticity, $E_{0.05}$, 5400 N/mm²Shear modulus of elasticity, G_{mean} , 500 N/mm²Characteristic density, ρ_k , 310 kg/m³Mean density, ρ_{mean} , 370 kg/m³

Span details

Bearing length $L_b = 100$ mm

Consider Combination 1 - 1.35G + 1.50Q (Strength)

Modification factors

Duration of load and moisture content - Table 3.1 $k_{mod} = 0.8$ Deformation factor - Table 3.2 $k_{def} = 0.8$ Depth factor for bending - Major axis - exp.3.1 $k_{h,m,y} = \min((150 \text{ mm} / h)^{0.2}, 1.3) = 1.064$ Bending stress re-distribution factor - cl.6.1.6(2) $k_m = 0.7$ Crack factor for shear resistance - cl.6.1.7(2) $k_{cr} = 0.67$ System strength factor - cl.6.6 $k_{sys} = 1.1$

Check compression parallel to the grain - cl.6.1.4

Design axial compression	$P_d = 2.233 \text{ kN}$
Design compressive stress	$\sigma_{c,0,d} = P_d / A = 0.406 \text{ N/mm}^2$
Design compressive strength	$f_{c,0,d} = k_{mod} \times k_{sys} \times f_{c,0,k} / \gamma_M = 11.508 \text{ N/mm}^2$
	$\sigma_{c,0,d} / f_{c,0,d} = 0.035$

PASS - Design parallel compression strength exceeds design parallel compression stress**Check design at start of span****Check compression perpendicular to the grain - cl.6.1.5**

Design perpendicular compression - major axis	$F_{c,y,90,d} = 2.218 \text{ kN}$
Effective contact length	$L_{b,ef} = L_b + \min(L_b, 30 \text{ mm}) = 130 \text{ mm}$
Design perpendicular compressive stress - exp.6.4	$\sigma_{c,y,90,d} = F_{c,y,90,d} / (b \times L_{b,ef}) = 0.341 \text{ N/mm}^2$
Design perpendicular compressive strength	$f_{c,y,90,d} = k_{mod} \times k_{sys} \times f_{c,90,k} / \gamma_M = 1.489 \text{ N/mm}^2$
	$\sigma_{c,y,90,d} / (k_{c,90} \times f_{c,y,90,d}) = 0.229$

PASS - Design perpendicular compression strength exceeds design perpendicular compression stress**Check shear force - Section 6.1.7**

Design shear force	$F_{y,d} = 0.349 \text{ kN}$
Design shear stress - exp.6.60	$\tau_{y,d} = 1.5 \times F_{y,d} / (k_{cr} \times b \times h) = 0.142 \text{ N/mm}^2$
Design shear strength	$f_{v,y,d} = k_{mod} \times k_{sys} \times f_{v,k} / \gamma_M = 2.166 \text{ N/mm}^2$
	$\tau_{y,d} / f_{v,y,d} = 0.066$

PASS - Design shear strength exceeds design shear stress**Check columns subjected to either compression or combined compression and bending - cl.6.3.2**

Effective length for y-axis bending	$L_{e,y} = 0.9 \times 1700 \text{ mm} = 1530 \text{ mm}$
Slenderness ratio	$\lambda_y = L_{e,y} / i_y = 48.183$
Relative slenderness ratio - exp. 6.21	$\lambda_{rel,y} = \lambda_y / \pi \times \sqrt{f_{c,0,k} / E_{0.05}} = 0.861$
Effective length for z-axis bending	$L_{e,z} = 0 \text{ mm}$
Slenderness ratio	$\lambda_z = L_{e,z} / i_z = 0$
Relative slenderness ratio - exp. 6.22	$\lambda_{rel,z} = \lambda_z / \pi \times \sqrt{f_{c,0,k} / E_{0.05}} = 0$
	$\lambda_{rel,y} > 0.3$ column stability check is required
Straightness factor	$\beta_c = 0.2$
Instability factors - exp.6.25, 6.26, 6.27 & 6.28	$k_y = 0.5 \times (1 + \beta_c \times (\lambda_{rel,y} - 0.3) + \lambda_{rel,y}^2) = 0.926$
	$k_z = 0.5 \times (1 + \beta_c \times (\lambda_{rel,z} - 0.3) + \lambda_{rel,z}^2) = 0.470$
	$k_{c,y} = 1 / (k_y + \sqrt{(k_y^2 - \lambda_{rel,y}^2)}) = 0.788$
	$k_{c,z} = 1 / (k_z + \sqrt{(k_z^2 - \lambda_{rel,z}^2)}) = 1.064$
Column stability checks - exp.6.23 & 6.24	$\sigma_{c,0,d} / (k_{c,y} \times f_{c,0,d}) = 0.045$
	$\sigma_{c,0,d} / (k_{c,z} \times f_{c,0,d}) = 0.033$

PASS - Column stability is acceptable**Check design at end of span****Check compression perpendicular to the grain - cl.6.1.5**

Design perpendicular compression - major axis	$F_{c,y,90,d} = 2.06 \text{ kN}$
Effective contact length	$L_{b,ef} = \min(L_b, 30 \text{ mm}) + L_b + \min(L_b, 30 \text{ mm}) = 160 \text{ mm}$
Design perpendicular compressive stress - exp.6.4	$\sigma_{c,y,90,d} = F_{c,y,90,d} / (b \times L_{b,ef}) = 0.258 \text{ N/mm}^2$
Design perpendicular compressive strength	$f_{c,y,90,d} = k_{mod} \times k_{sys} \times f_{c,90,k} / \gamma_M = 1.489 \text{ N/mm}^2$

$$\sigma_{c,y,90,d} / (k_{c,90} \times f_{c,y,90,d}) = \mathbf{0.173}$$

PASS - Design perpendicular compression strength exceeds design perpendicular compression stress

Check shear force - Section 6.1.7

Design shear force

$$F_{y,d} = \mathbf{0.912 \text{ kN}}$$

Design shear stress - exp.6.60

$$\tau_{y,d} = 1.5 \times F_{y,d} / (k_{cr} \times b \times h) = \mathbf{0.371 \text{ N/mm}^2}$$

Design shear strength

$$f_{v,y,d} = k_{mod} \times k_{sys} \times f_{v,k} / \gamma_M = \mathbf{2.166 \text{ N/mm}^2}$$

$$\tau_{y,d} / f_{v,y,d} = \mathbf{0.171}$$

PASS - Design shear strength exceeds design shear stress

Check bending moment - Section 6.1.6

Design bending moment

$$M_{y,d} = \mathbf{0.479 \text{ kNm}}$$

Design bending stress

$$\sigma_{m,y,d} = M_{y,d} / W_y = \mathbf{4.747 \text{ N/mm}^2}$$

Design bending strength

$$f_{m,y,d} = k_{h,m,y} \times k_{mod} \times k_{sys} \times f_{m,k} / \gamma_M = \mathbf{11.524 \text{ N/mm}^2}$$

$$\sigma_{m,y,d} / f_{m,y,d} = \mathbf{0.412}$$

PASS - Design bending strength exceeds design bending stress

Check combined bending and axial compression - Section 6.2.4

Combined loading checks - exp.6.19 & 6.20

$$(\sigma_{c,0,d} / f_{c,0,d})^2 + \sigma_{m,y,d} / f_{m,y,d} = \mathbf{0.413}$$

$$(\sigma_{c,0,d} / f_{c,0,d})^2 + k_m \times \sigma_{m,y,d} / f_{m,y,d} = \mathbf{0.290}$$

PASS - Combined bending and axial compression utilisation is acceptable

Check columns subjected to either compression or combined compression and bending - cl.6.3.2

Effective length for y-axis bending

$$L_{e,y} = 0.9 \times 1700 \text{ mm} = \mathbf{1530 \text{ mm}}$$

Slenderness ratio

$$\lambda_y = L_{e,y} / i_y = \mathbf{48.183}$$

Relative slenderness ratio - exp. 6.21

$$\lambda_{rel,y} = \lambda_y / \pi \times \sqrt{(f_{c,0,k} / E_{0.05})} = \mathbf{0.861}$$

Effective length for z-axis bending

$$L_{e,z} = \mathbf{0 \text{ mm}}$$

Slenderness ratio

$$\lambda_z = L_{e,z} / i_z = \mathbf{0}$$

Relative slenderness ratio - exp. 6.22

$$\lambda_{rel,z} = \lambda_z / \pi \times \sqrt{(f_{c,0,k} / E_{0.05})} = \mathbf{0}$$

$\lambda_{rel,y} > 0.3$ column stability check is required

Straightness factor

$$\beta_c = \mathbf{0.2}$$

Instability factors - exp.6.25, 6.26, 6.27 & 6.28

$$k_y = 0.5 \times (1 + \beta_c \times (\lambda_{rel,y} - 0.3) + \lambda_{rel,y}^2) = \mathbf{0.926}$$

$$k_z = 0.5 \times (1 + \beta_c \times (\lambda_{rel,z} - 0.3) + \lambda_{rel,z}^2) = \mathbf{0.470}$$

$$k_{c,y} = 1 / (k_y + \sqrt{(k_y^2 - \lambda_{rel,y}^2)}) = \mathbf{0.788}$$

$$k_{c,z} = 1 / (k_z + \sqrt{(k_z^2 - \lambda_{rel,z}^2)}) = \mathbf{1.064}$$

Column stability checks - exp.6.23 & 6.24

$$\sigma_{c,0,d} / (k_{c,y} \times f_{c,0,d}) + \sigma_{m,y,d} / f_{m,y,d} = \mathbf{0.457}$$

$$\sigma_{c,0,d} / (k_{c,z} \times f_{c,0,d}) + k_m \times \sigma_{m,y,d} / f_{m,y,d} = \mathbf{0.322}$$

PASS - Column stability is acceptable

Check beams subjected to either bending or combined bending and compression - cl.6.3.3

Lateral buckling factor - exp.6.34

$$k_{crit} = \mathbf{1.000}$$

Beam stability check - exp.6.35

$$(\sigma_{m,y,d} / (k_{crit} \times f_{m,y,d}))^2 + \sigma_{c,0,d} / (k_{c,z} \times f_{c,0,d}) = \mathbf{0.203}$$

PASS - Beam stability is acceptable

Consider Combination 2 - 1.00G + 1.00Q (Service)

Check design 1374 mm along span

Check y-y axis deflection - Section 7.2

Instantaneous deflection

$$\delta_y = \mathbf{0.2 \text{ mm}}$$

ANALYSIS & DESIGN

PITCHED ROOF RAFTERS

Quasi-permanent variable load factor

$$\psi_2 = 0.3$$

Final deflection with creep

$$\delta_{y,Final} = \delta_y \times (1 + k_{def}) = 0.4 \text{ mm}$$

Allowable deflection

$$\delta_{y,Allowable} = L_{m1_s1} / 250 = 6.8 \text{ mm}$$

$$\delta_{y,Final} / \delta_{y,Allowable} = 0.065$$

PASS - Allowable deflection exceeds final deflection

Member - Span 2

Partial factor for material properties and resistances

Partial factor for material properties - Table 2.3

$$\gamma_M = 1.300$$

Member details

Load duration - cl.2.3.1.2

Medium-term

Service class - cl.2.3.1.3

2

Timber section details

Number of timber sections in member

$$N = 1$$

Breadth of sections

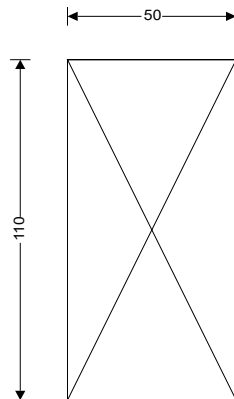
$$b = 50 \text{ mm}$$

Depth of sections

$$h = 110 \text{ mm}$$

Timber strength class - EN 338:2016 Table 1

C16



50x110 timber section

Cross-sectional area, A , 5500 mm²Section modulus, W_y , 100833.3 mm³Section modulus, W_z , 45833 mm³Second moment of area, I_y , 5545833 mm⁴Second moment of area, I_z , 1145833 mm⁴Radius of gyration, i_y , 31.8 mmRadius of gyration, i_z , 14.4 mm

Timber strength class C16

Characteristic bending strength, $f_{m,k}$, 16 N/mm²Characteristic shear strength, $f_{v,k}$, 3.2 N/mm²Characteristic compression strength parallel to grain, $f_{c,0,k}$, 17 N/mm²Characteristic compression strength perpendicular to grain, $f_{c,90,k}$, 2.2 N/mm²Characteristic tension strength parallel to grain, $f_{t,0,k}$, 8.5 N/mm²Mean modulus of elasticity, $E_{0,mean}$, 8000 N/mm²Fifth percentile modulus of elasticity, $E_{0.05}$, 5400 N/mm²Shear modulus of elasticity, G_{mean} , 500 N/mm²Characteristic density, ρ_k , 310 kg/m³Mean density, ρ_{mean} , 370 kg/m³

Span details

Bearing length

$$L_b = 100 \text{ mm}$$

Consider Combination 1 - 1.35G + 1.50Q (Strength)

Modification factors

Duration of load and moisture content - Table 3.1

$$k_{mod} = 0.8$$

Deformation factor - Table 3.2

$$k_{def} = 0.8$$

Depth factor for bending - Major axis - exp.3.1

$$k_{h,m,y} = \min((150 \text{ mm} / h)^{0.2}, 1.3) = 1.064$$

Bending stress re-distribution factor - cl.6.1.6(2)

$$k_m = 0.7$$

Crack factor for shear resistance - cl.6.1.7(2)

$$k_{cr} = 0.67$$

System strength factor - cl.6.6

$$k_{sys} = 1.1$$

Check compression parallel to the grain - cl.6.1.4

Design axial compression

$$P_d = 1.35 \text{ kN}$$

Design compressive stress

$$\sigma_{c,0,d} = P_d / A = 0.246 \text{ N/mm}^2$$

Design compressive strength

$$f_{c,0,d} = k_{mod} \times k_{sys} \times f_{c,0,k} / \gamma_M = 11.508 \text{ N/mm}^2$$

$$\sigma_{c,0,d} / f_{c,0,d} = 0.021$$

PASS - Design parallel compression strength exceeds design parallel compression stress

Check design at start of span

Check compression perpendicular to the grain - cl.6.1.5

Design perpendicular compression - major axis $F_{c,y,90,d} = 2.06 \text{ kN}$
 Effective contact length $L_{b,ef} = \min(L_b, 30 \text{ mm}) + L_b + \min(L_b, 30 \text{ mm}) = 160 \text{ mm}$
 Design perpendicular compressive stress - exp.6.4 $\sigma_{c,y,90,d} = F_{c,y,90,d} / (b \times L_{b,ef}) = 0.258 \text{ N/mm}^2$
 Design perpendicular compressive strength $f_{c,y,90,d} = k_{mod} \times k_{sys} \times f_{c,90,k} / \gamma_M = 1.489 \text{ N/mm}^2$
 $\sigma_{c,y,90,d} / (k_{c,90} \times f_{c,y,90,d}) = 0.173$

PASS - Design perpendicular compression strength exceeds design perpendicular compression stress

Check shear force - Section 6.1.7

Design shear force $F_{y,d} = 1.148 \text{ kN}$
 Design shear stress - exp.6.60 $\tau_{y,d} = 1.5 \times F_{y,d} / (k_{cr} \times b \times h) = 0.467 \text{ N/mm}^2$
 Design shear strength $f_{v,y,d} = k_{mod} \times k_{sys} \times f_{v,k} / \gamma_M = 2.166 \text{ N/mm}^2$
 $\tau_{y,d} / f_{v,y,d} = 0.216$

PASS - Design shear strength exceeds design shear stress

Check bending moment - Section 6.1.6

Design bending moment $M_{y,d} = 0.479 \text{ kNm}$
 Design bending stress $\sigma_{m,y,d} = M_{y,d} / W_y = 4.747 \text{ N/mm}^2$
 Design bending strength $f_{m,y,d} = k_{h,m,y} \times k_{mod} \times k_{sys} \times f_{m,k} / \gamma_M = 11.524 \text{ N/mm}^2$
 $\sigma_{m,y,d} / f_{m,y,d} = 0.412$

PASS - Design bending strength exceeds design bending stress

Check combined bending and axial compression - Section 6.2.4

Combined loading checks - exp.6.19 & 6.20 $(\sigma_{c,0,d} / f_{c,0,d})^2 + \sigma_{m,y,d} / f_{m,y,d} = 0.412$
 $(\sigma_{c,0,d} / f_{c,0,d})^2 + k_m \times \sigma_{m,y,d} / f_{m,y,d} = 0.289$

PASS - Combined bending and axial compression utilisation is acceptable

Check columns subjected to either compression or combined compression and bending - cl.6.3.2

Effective length for y-axis bending $L_{e,y} = 0.9 \times 2600 \text{ mm} = 2340 \text{ mm}$
 Slenderness ratio $\lambda_y = L_{e,y} / i_y = 73.691$
 Relative slenderness ratio - exp. 6.21 $\lambda_{rel,y} = \lambda_y / \pi \times \sqrt{f_{c,0,k} / E_{0.05}} = 1.316$
 Effective length for z-axis bending $L_{e,z} = 0 \text{ mm}$
 Slenderness ratio $\lambda_z = L_{e,z} / i_z = 0$
 Relative slenderness ratio - exp. 6.22 $\lambda_{rel,z} = \lambda_z / \pi \times \sqrt{f_{c,0,k} / E_{0.05}} = 0$
 $\lambda_{rel,y} > 0.3$ column stability check is required

Straightness factor $\beta_c = 0.2$
 Instability factors - exp.6.25, 6.26, 6.27 & 6.28 $k_y = 0.5 \times (1 + \beta_c \times (\lambda_{rel,y} - 0.3) + \lambda_{rel,y}^2) = 1.468$
 $k_z = 0.5 \times (1 + \beta_c \times (\lambda_{rel,z} - 0.3) + \lambda_{rel,z}^2) = 0.470$
 $k_{c,y} = 1 / (k_y + \sqrt{k_y^2 - \lambda_{rel,y}^2}) = 0.472$
 $k_{c,z} = 1 / (k_z + \sqrt{k_z^2 - \lambda_{rel,z}^2}) = 1.064$
 Column stability checks - exp.6.23 & 6.24 $\sigma_{c,0,d} / (k_{c,y} \times f_{c,0,d}) + \sigma_{m,y,d} / f_{m,y,d} = 0.457$
 $\sigma_{c,0,d} / (k_{c,z} \times f_{c,0,d}) + k_m \times \sigma_{m,y,d} / f_{m,y,d} = 0.308$

PASS - Column stability is acceptable

ANALYSIS & DESIGN

PITCHED ROOF RAFTERS

Check beams subjected to either bending or combined bending and compression - cl.6.3.3

Lateral buckling factor - exp.6.34

$$k_{crit} = 1.000$$

Beam stability check - exp.6.35

$$(\sigma_{m,y,d} / (k_{crit} \times f_{m,y,d}))^2 + \sigma_{c,0,d} / (k_{c,z} \times f_{c,0,d}) = 0.19$$

PASS - Beam stability is acceptable

Consider Combination 2 - 1.00G + 1.00Q (Service)

Check design 1426 mm along span

Check y-y axis deflection - Section 7.2

Instantaneous deflection

$$\delta_y = 4.1 \text{ mm}$$

Quasi-permanent variable load factor

$$\psi_2 = 0.3$$

Final deflection with creep

$$\delta_{y,Final} = \delta_y \times (1 + k_{def}) = 7.4 \text{ mm}$$

Allowable deflection

$$\delta_{y,Allowable} = L_{m1_s2} / 250 = 10.4 \text{ mm}$$

$$\delta_{y,Final} / \delta_{y,Allowable} = 0.716$$

PASS - Allowable deflection exceeds final deflection

LOADS CALCULATIONS
RIDGE BEAM RB1

Flat Roof Loads		
Item	Unfactored Load (KN/m ²)	Load Type
Chippings and Felt	0.3	Dead
Board, Joists & Firrings	0.3	Dead
Ceiling & Insulation	0.25	Dead
ROOF DEAD LOAD ON PLAN		0.85 (KN/m2)
ROOF LIVE LOAD ON PLAN		0.75 (KN/m2)

Pitched Roof Loads		
Item	Unfactored Load (KN/m ²)	Load Type
Roof Tiles	0.6	Dead
Rafters	0.15	Dead
Felt & Battens	0.1	Dead
Insulation	0.1	Dead
Plasterboard	0.15	Dead
ROOF DEAD LOAD ON PLAN		1.36 (KN/m2)
ROOF LIVE LOAD ON PLAN		0.5 (KN/m2)

Proposed UDLs				
Item	Span (m)	Dead Load (KN/m ²)	Live Load (KN/m ²)	Comments
Flat Roof	1.7	0.85	0.75	See Load Table For Flat Roof
Pitched Roof	1	1.36	0.5	See Load Table For Pitched Roof
Total Dead		2.81 (KN/m)		
Total Live		1.78 (KN/m)		

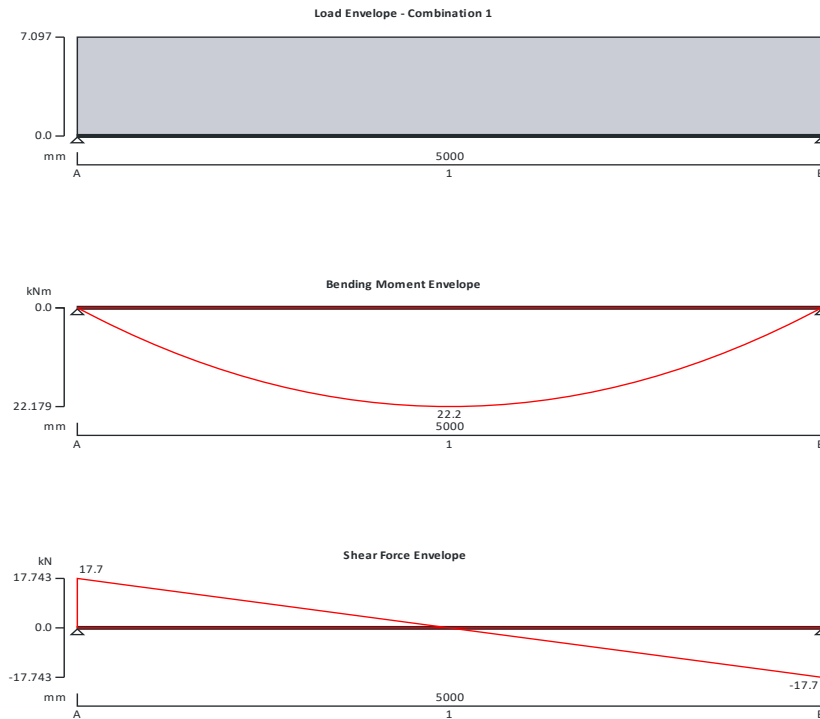
ANALYSIS & DESIGN

RIDGE BEAM RB1

STEEL BEAM ANALYSIS & DESIGN (BS5950)

In accordance with BS5950-1:2000 incorporating Corrigendum No.1

TEDDS calculation version 3.0.08



Support conditions

Support A

Vertically restrained

Rotationally free

Support B

Vertically restrained

Rotationally free

Applied loading

Beam loads

Dead self weight of beam $\times 1$

Dead full UDL 2.81 kN/m

Imposed full UDL 1.78 kN/m

Load combinations

Load combination 1

Support A

Dead $\times 1.40$

Imposed $\times 1.60$

Dead $\times 1.40$

Imposed $\times 1.60$

Support B

Dead $\times 1.40$

Imposed $\times 1.60$

Analysis results

Maximum moment

$M_{\max} = 22.2 \text{ kNm}$

$M_{\min} = 0 \text{ kNm}$

Maximum shear

$V_{\max} = 17.7 \text{ kN}$

$V_{\min} = -17.7 \text{ kN}$

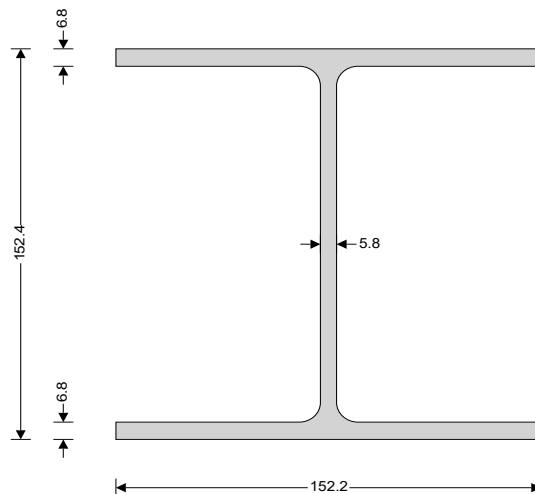
ANALYSIS & DESIGN

RIDGE BEAM RB1

Deflection	$\delta_{\max} = 15.3 \text{ mm}$	$\delta_{\min} = 0 \text{ mm}$
Maximum reaction at support A	$R_{A_{\max}} = 17.7 \text{ kN}$	$R_{A_{\min}} = 17.7 \text{ kN}$
Unfactored dead load reaction at support A	$R_{A_{\text{Dead}}} = 7.6 \text{ kN}$	
Unfactored imposed load reaction at support A	$R_{A_{\text{Imposed}}} = 4.5 \text{ kN}$	
Maximum reaction at support B	$R_{B_{\max}} = 17.7 \text{ kN}$	$R_{B_{\min}} = 17.7 \text{ kN}$
Unfactored dead load reaction at support B	$R_{B_{\text{Dead}}} = 7.6 \text{ kN}$	
Unfactored imposed load reaction at support B	$R_{B_{\text{Imposed}}} = 4.5 \text{ kN}$	

Section details

Section type	UC 152x152x23 (British Steel Section Range 2022)
(BS4-1))	
Steel grade	S275
From table 9: Design strength p_y	
Thickness of element	$\max(T, t) = 6.8 \text{ mm}$
Design strength	$p_y = 275 \text{ N/mm}^2$
Modulus of elasticity	$E = 205000 \text{ N/mm}^2$



Lateral restraint

Span 1 has lateral restraint at supports only

Effective length factors

Effective length factor in major axis	$K_x = 1.00$
Effective length factor in minor axis	$K_y = 1.00$
Effective length factor for lateral-torsional buckling	$K_{LT,A} = 1.00 + 2 \times D$
	$K_{LT,B} = 1.00 + 2 \times D$

Classification of cross sections - Section 3.5

$$\varepsilon = \sqrt{[275 \text{ N/mm}^2 / p_y]} = 1.00$$

Internal compression parts - Table 11

Depth of section	$d = 123.6 \text{ mm}$	
	$d / t = 21.3 \times \varepsilon \leq 80 \times \varepsilon$	Class 1 plastic

Outstand flanges - Table 11

Width of section	$b = B / 2 = 76.1 \text{ mm}$
------------------	-------------------------------

compact $b / T = 11.2 \times \varepsilon \leq 15 \times \varepsilon$ Class 3 semi-

Section is class 3 semi-compact

Shear capacity - Section 4.2.3

Design shear force

$$F_v = \max(\text{abs}(V_{\max}), \text{abs}(V_{\min})) = 17.7 \text{ kN}$$

$$d / t < 70 \times \varepsilon$$

Web does not need to be checked for shear buckling

Shear area

$$A_v = t \times D = 884 \text{ mm}^2$$

Design shear resistance

$$P_v = 0.6 \times p_y \times A_v = 145.8 \text{ kN}$$

PASS - Design shear resistance exceeds design shear force

Moment capacity - Section 4.2.5

Design bending moment

$$M = \max(\text{abs}(M_{s1_max}), \text{abs}(M_{s1_min})) = 22.2 \text{ kNm}$$

Effective plastic modulus - Section 3.5.6

Limiting value for class 2 compact flange

$$\beta_{2f} = 10 \times \varepsilon = 10$$

Limiting value for class 3 semi-compact flange

$$\beta_{3f} = 15 \times \varepsilon = 15$$

Limiting value for class 2 compact web

$$\beta_{2w} = 100 \times \varepsilon = 100$$

Limiting value for class 3 semi-compact web

$$\beta_{3w} = 120 \times \varepsilon = 120$$

Effective plastic modulus - cl.3.5.6.2

$$S_{\text{eff}} = \min(Z_{xx} + (S_{xx} - Z_{xx}) \times \min(\frac{[(\beta_{3w} / (d / t))^2 - 1]}{[(\beta_{3w} / \beta_{2w})^2 - 1]}, \frac{[(\beta_{3f} / (b / T) - 1)}{(\beta_{3f} / \beta_{2f} - 1)}]), S_{xx}) = 176245 \text{ mm}^3$$

Moment capacity low shear - cl.4.2.5.2

$$M_c = \min(p_y \times S_{\text{eff}}, 1.2 \times p_y \times Z_{xx}) = 48.5 \text{ kNm}$$

Effective length for lateral-torsional buckling - Section 4.3.5

Effective length for lateral torsional buckling

$$L_E = 1.0 \times L_{s1} + 2 \times D = 5305 \text{ mm}$$

Slenderness ratio

$$\lambda = L_E / r_{yy} = 143.454$$

Equivalent slenderness - Section 4.3.6.7

Buckling parameter

$$u = 0.840$$

Torsional index

$$x = 20.701$$

Slenderness factor

$$v = 1 / [1 + 0.05 \times (\lambda / x)^2]^{0.25} = 0.736$$

Ratio - cl.4.3.6.9

$$\beta_w = S_{\text{eff}} / S_{xx} = 0.968$$

Equivalent slenderness - cl.4.3.6.7

$$\lambda_{LT} = u \times v \times \lambda \times \sqrt{\beta_w} = 87.277$$

Limiting slenderness - Annex B.2.2

$$\lambda_{L0} = 0.4 \times (\pi^2 \times E / p_y)^{0.5} = 34.310$$

$\lambda_{LT} > \lambda_{L0}$ - Allowance should be made for lateral-torsional buckling

Bending strength - Section 4.3.6.5

Robertson constant

$$\alpha_{LT} = 7.0$$

Perry factor

$$\eta_{LT} = \max(\alpha_{LT} \times (\lambda_{LT} - \lambda_{L0}) / 1000, 0) = 0.371$$

Euler stress

$$p_E = \pi^2 \times E / \lambda_{LT}^2 = 265.6 \text{ N/mm}^2$$

$$\phi_{LT} = (p_y + (\eta_{LT} + 1) \times p_E) / 2 = 319.5 \text{ N/mm}^2$$

Bending strength - Annex B.2.1

$$p_b = p_E \times p_y / (\phi_{LT} + (\phi_{LT}^2 - p_E \times p_y)^{0.5}) = 149.1 \text{ N/mm}^2$$

Equivalent uniform moment factor - Section 4.3.6.6

Moment at quarter point of segment

$$M_2 = 16.6 \text{ kNm}$$

Moment at centre-line of segment

$$M_3 = 22.2 \text{ kNm}$$

Moment at three quarter point of segment

$$M_4 = 16.6 \text{ kNm}$$

Maximum moment in segment

$$M_{\text{abs}} = 22.2 \text{ kNm}$$

Maximum moment governing buckling resistance

$$M_{LT} = M_{\text{abs}} = 22.2 \text{ kNm}$$

Equivalent uniform moment factor for lateral-torsional buckling

$$m_{LT} = \max(0.2 + (0.15 \times M_2 + 0.5 \times M_3 + 0.15 \times M_4) / M_{abs}, 0.44) = \mathbf{0.925}$$

Buckling resistance moment - Section 4.3.6.4

Buckling resistance moment

$$M_b = p_b \times S_{eff} = \mathbf{26.3 \text{ kNm}}$$

$$M_b / m_{LT} = \mathbf{28.4 \text{ kNm}}$$

PASS - Buckling resistance moment exceeds design bending moment

Check vertical deflection - Section 2.5.2

Consider deflection due to dead and imposed loads

Limiting deflection

$$\delta_{lim} = L_{s1} / 250 = \mathbf{20 \text{ mm}}$$

Maximum deflection span 1

$$\delta = \max(\text{abs}(\delta_{max}), \text{abs}(\delta_{min})) = \mathbf{15.294 \text{ mm}}$$

PASS - Maximum deflection does not exceed deflection limit

LOADS CALCULATIONS

BEAM B2

Pitched Roof Loads		
Item	Unfactored Load (KN/m²)	Load Type
Roof Tiles	0.6	Dead
Rafters	0.15	Dead
Felt & Battens	0.1	Dead
Insulation	0.1	Dead
Plasterboard	0.15	Dead
ROOF DEAD LOAD ON PLAN		1.36 (KN/m²)
ROOF LIVE LOAD ON PLAN		0.5 (KN/m²)

Timber Joists - Internal Floor Loads		
Item	Unfactored Load (KN/m²)	Load Type
Floor joists	0.15	Dead
Floor boards	0.05	Dead
Plaster board and Skim	0.25	Dead
Finish	0.05	Dead
Residential Live Loading	1.5	Live
TOTAL FLOOR DEAD LOAD		0.5 (KN/m²)
TOTAL FLOOR LIVE LOAD		1.5 (KN/m²)

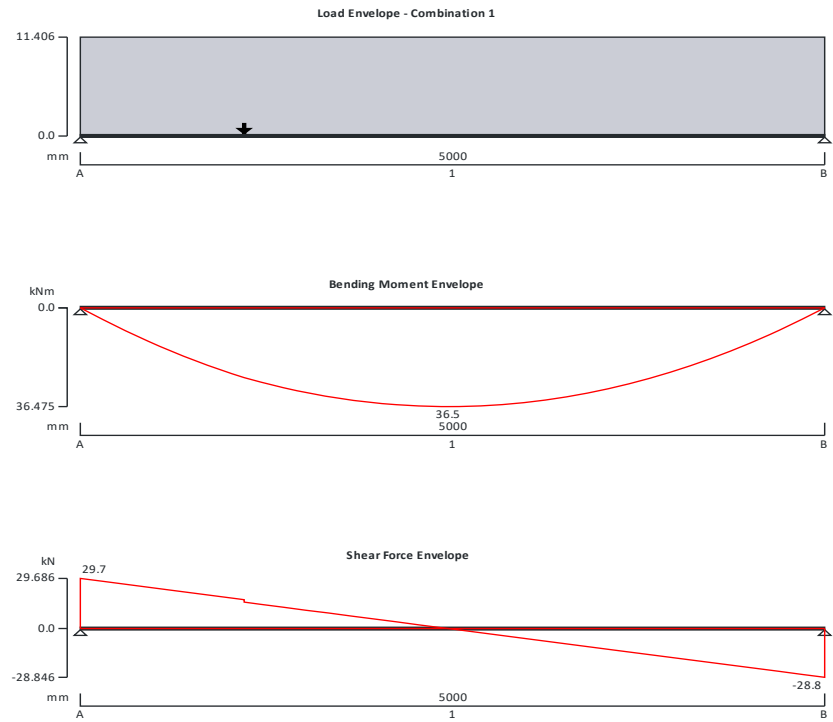
Proposed UDLs				
Item	Span (m)	Dead Load (KN/m²)	Live Load (KN/m²)	Comments
Pitched Roof	1.7	1.36	0.5	See Load Table For Pitched Roof
Loft Floor Loading	1.45	0.5	1.5	See Load Table For Internal Floor
Timber Walls	1.35	1	0	1 KN/m ² assumed for timber construction
T2 Reaction	-	-	-	1.5 KN @ 1100mm
Total Dead			4.39 (KN/m)	
Total Live			3.03 (KN/m)	

ANALYSIS & DESIGN
BEAM B2

STEEL BEAM ANALYSIS & DESIGN (BS5950)

In accordance with BS5950-1:2000 incorporating Corrigendum No.1

TEDDS calculation version 3.0.08



Support conditions

Support A

Vertically restrained

Rotationally free

Support B

Vertically restrained

Rotationally free

Applied loading

Beam loads

Dead self weight of beam $\times 1$

Dead full UDL 4.39 kN/m

Imposed full UDL 3.03 kN/m

Other point load 1.5 kN at 1100 mm

Load combinations

Load combination 1

Support A

Dead $\times 1.40$

Imposed $\times 1.60$

Other $\times 1.00$

Dead $\times 1.40$

Imposed $\times 1.60$

Other $\times 1.00$

Support B

Dead $\times 1.40$

Imposed $\times 1.60$

ANALYSIS & DESIGN

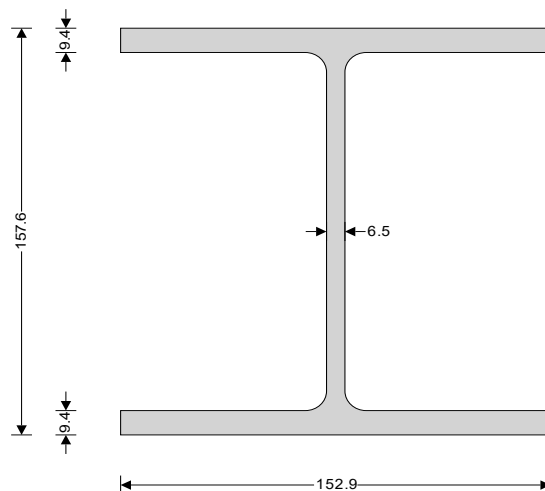
BEAM B2

Other $\times 1.00$ **Analysis results**

Maximum moment	$M_{\max} = 36.5 \text{ kNm}$	$M_{\min} = 0 \text{ kNm}$
Maximum shear	$V_{\max} = 29.7 \text{ kN}$	$V_{\min} = -28.8 \text{ kN}$
Deflection	$\delta_{\max} = 18.2 \text{ mm}$	$\delta_{\min} = 0 \text{ mm}$
Maximum reaction at support A	$R_{A_{\max}} = 29.7 \text{ kN}$	$R_{A_{\min}} = 29.7 \text{ kN}$
Unfactored dead load reaction at support A	$R_{A_{\text{Dead}}} = 11.7 \text{ kN}$	
Unfactored imposed load reaction at support A	$R_{A_{\text{Imposed}}} = 7.6 \text{ kN}$	
Unfactored other load reaction at support A	$R_{A_{\text{Other}}} = 1.2 \text{ kN}$	
Maximum reaction at support B	$R_{B_{\max}} = 28.8 \text{ kN}$	$R_{B_{\min}} = 28.8 \text{ kN}$
Unfactored dead load reaction at support B	$R_{B_{\text{Dead}}} = 11.7 \text{ kN}$	
Unfactored imposed load reaction at support B	$R_{B_{\text{Imposed}}} = 7.6 \text{ kN}$	
Unfactored other load reaction at support B	$R_{B_{\text{Other}}} = 0.3 \text{ kN}$	

Section details

Section type	UC 152x152x30 (British Steel Section Range 2022)
(BS4-1))	
Steel grade	S275
From table 9: Design strength p_y	
Thickness of element	$\max(T, t) = 9.4 \text{ mm}$
Design strength	$p_y = 275 \text{ N/mm}^2$
Modulus of elasticity	$E = 205000 \text{ N/mm}^2$

**Lateral restraint**

Span 1 has lateral restraint at supports only

Effective length factors

Effective length factor in major axis	$K_x = 1.00$
Effective length factor in minor axis	$K_y = 1.00$
Effective length factor for lateral-torsional buckling	$K_{LT,A} = 1.00 + 2 \times D$
	$K_{LT,B} = 1.00 + 2 \times D$

Classification of cross sections - Section 3.5

$$\varepsilon = \sqrt{[275 \text{ N/mm}^2 / p_y]} = 1.00$$

ANALYSIS & DESIGN

BEAM B2

Internal compression parts - Table 11

Depth of section	$d = 123.6 \text{ mm}$	
	$d / t = 19.0 \times \varepsilon \leq 80 \times \varepsilon$	Class 1 plastic

Outstand flanges - Table 11

Width of section	$b = B / 2 = 76.5 \text{ mm}$	
	$b / T = 8.1 \times \varepsilon \leq 9 \times \varepsilon$	Class 1 plastic

Section is class 1 plastic**Shear capacity - Section 4.2.3**

Design shear force	$F_v = \max(\text{abs}(V_{\max}), \text{abs}(V_{\min})) = 29.7 \text{ kN}$
	$d / t < 70 \times \varepsilon$
	Web does not need to be checked for shear buckling
Shear area	$A_v = t \times D = 1024 \text{ mm}^2$
Design shear resistance	$P_v = 0.6 \times p_y \times A_v = 169 \text{ kN}$
	PASS - Design shear resistance exceeds design shear force

Moment capacity - Section 4.2.5

Design bending moment	$M = \max(\text{abs}(M_{s1_max}), \text{abs}(M_{s1_min})) = 36.5 \text{ kNm}$
Moment capacity low shear - cl.4.2.5.2	$M_c = \min(p_y \times S_{xx}, 1.2 \times p_y \times Z_{xx}) = 68.1 \text{ kNm}$

Effective length for lateral-torsional buckling - Section 4.3.5

Effective length for lateral torsional buckling	$L_E = 1.0 \times L_{s1} + 2 \times D = 5315 \text{ mm}$
Slenderness ratio	$\lambda = L_E / r_{yy} = 138.879$

Equivalent slenderness - Section 4.3.6.7

Buckling parameter	$u = 0.849$
Torsional index	$\chi = 15.999$
Slenderness factor	$v = 1 / [1 + 0.05 \times (\lambda / \chi)^2]^{0.25} = 0.677$
Ratio - cl.4.3.6.9	$\beta_w = 1.000$
Equivalent slenderness - cl.4.3.6.7	$\lambda_{LT} = u \times v \times \lambda \times \sqrt{[\beta_w]} = 79.748$
Limiting slenderness - Annex B.2.2	$\lambda_{L0} = 0.4 \times (\pi^2 \times E / p_y)^{0.5} = 34.310$

 $\lambda_{LT} > \lambda_{L0}$ - Allowance should be made for lateral-torsional buckling**Bending strength - Section 4.3.6.5**

Robertson constant	$\alpha_{LT} = 7.0$
Perry factor	$\eta_{LT} = \max(\alpha_{LT} \times (\lambda_{LT} - \lambda_{L0}) / 1000, 0) = 0.318$
Euler stress	$p_E = \pi^2 \times E / \lambda_{LT}^2 = 318.1 \text{ N/mm}^2$
	$\phi_{LT} = (p_y + (\eta_{LT} + 1) \times p_E) / 2 = 347.2 \text{ N/mm}^2$
Bending strength - Annex B.2.1	$p_b = p_E \times p_y / (\phi_{LT} + (\phi_{LT}^2 - p_E \times p_y)^{0.5}) = 165.4 \text{ N/mm}^2$

Equivalent uniform moment factor - Section 4.3.6.6

Moment at quarter point of segment	$M_2 = 28 \text{ kNm}$
Moment at centre-line of segment	$M_3 = 36.5 \text{ kNm}$
Moment at three quarter point of segment	$M_4 = 27.1 \text{ kNm}$
Maximum moment in segment	$M_{abs} = 36.5 \text{ kNm}$
Maximum moment governing buckling resistance	$M_{LT} = M_{abs} = 36.5 \text{ kNm}$
Equivalent uniform moment factor for lateral-torsional buckling	

$$m_{LT} = \max(0.2 + (0.15 \times M_2 + 0.5 \times M_3 + 0.15 \times M_4) / M_{abs}, 0.44) = 0.927$$

Buckling resistance moment - Section 4.3.6.4

Buckling resistance moment

$$M_b = p_b \times S_{xx} = 41 \text{ kNm}$$

$$M_b / m_{LT} = 44.2 \text{ kNm}$$

PASS - Buckling resistance moment exceeds design bending moment

Check vertical deflection - Section 2.5.2

Consider deflection due to dead, imposed and other loads

Limiting deflection

$$\delta_{lim} = L_{s1} / 250 = 20 \text{ mm}$$

Maximum deflection span 1

$$\delta = \max(\text{abs}(\delta_{max}), \text{abs}(\delta_{min})) = 18.205 \text{ mm}$$

PASS - Maximum deflection does not exceed deflection limit

LOADS CALCULATIONS

BEAM B3

Timber Joists - Internal Floor Loads		
Item	Unfactored Load (KN/m²)	Load Type
Floor joists	0.15	Dead
Floor boards	0.05	Dead
Plaster board and Skim	0.25	Dead
Finish	0.05	Dead
Residential Live Loading	1.5	Live
TOTAL FLOOR DEAD LOAD		0.5 (KN/m²)
TOTAL FLOOR LIVE LOAD		1.5 (KN/m²)

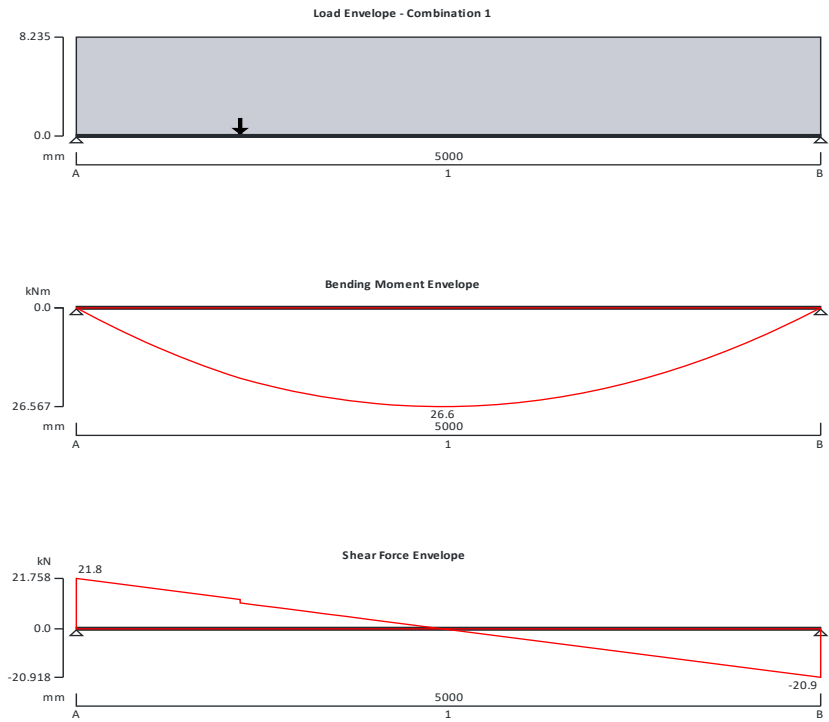
Proposed UDLs				
Item	Span (m)	Dead Load (KN/m²)	Live Load (KN/m²)	Comments
Loft Floor Loading	2.55	0.5	1.5	See Load Table For Internal Floor
T2 Reaction	-	-	-	1.5 KN @ 1100mm
Total Dead			1.28 (KN/m)	
Total Live			3.83 (KN/m)	

ANALYSIS & DESIGN
BEAM B3

STEEL BEAM ANALYSIS & DESIGN (BS5950)

In accordance with BS5950-1:2000 incorporating Corrigendum No.1

TEDDS calculation version 3.0.08



Support conditions

Support A

Vertically restrained

Rotationally free

Support B

Vertically restrained

Rotationally free

Applied loading

Beam loads

Dead self weight of beam $\times 1$

Dead full UDL 1.28 kN/m

Imposed full UDL 3.83 kN/m

Other point load 1.5 kN at 1100 mm

Load combinations

Load combination 1

Support A

Dead $\times 1.40$

Imposed $\times 1.60$

Other $\times 1.00$

Dead $\times 1.40$

Imposed $\times 1.60$

Other $\times 1.00$

Support B

Dead $\times 1.40$

Imposed $\times 1.60$

ANALYSIS & DESIGN

BEAM B3

Other $\times 1.00$ **Analysis results**

Maximum moment

$M_{\max} = 26.6 \text{ kNm}$

$M_{\min} = 0 \text{ kNm}$

Maximum shear

$V_{\max} = 21.8 \text{ kN}$

$V_{\min} = -20.9 \text{ kN}$

Deflection

$\delta_{\max} = 17.9 \text{ mm}$

$\delta_{\min} = 0 \text{ mm}$

Maximum reaction at support A

$R_{A_{\max}} = 21.8 \text{ kN}$

$R_{A_{\min}} = 21.8 \text{ kN}$

Unfactored dead load reaction at support A

$R_{A_{\text{Dead}}} = 3.8 \text{ kN}$

Unfactored imposed load reaction at support A

$R_{A_{\text{Imposed}}} = 9.6 \text{ kN}$

Unfactored other load reaction at support A

$R_{A_{\text{Other}}} = 1.2 \text{ kN}$

Maximum reaction at support B

$R_{B_{\max}} = 20.9 \text{ kN}$

$R_{B_{\min}} = 20.9 \text{ kN}$

Unfactored dead load reaction at support B

$R_{B_{\text{Dead}}} = 3.8 \text{ kN}$

Unfactored imposed load reaction at support B

$R_{B_{\text{Imposed}}} = 9.6 \text{ kN}$

Unfactored other load reaction at support B

$R_{B_{\text{Other}}} = 0.3 \text{ kN}$

Section details

Section type

UC 152x152x23 (British Steel Section Range 2022**(BS4-1))**

Steel grade

S275**From table 9: Design strength p_y**

Thickness of element

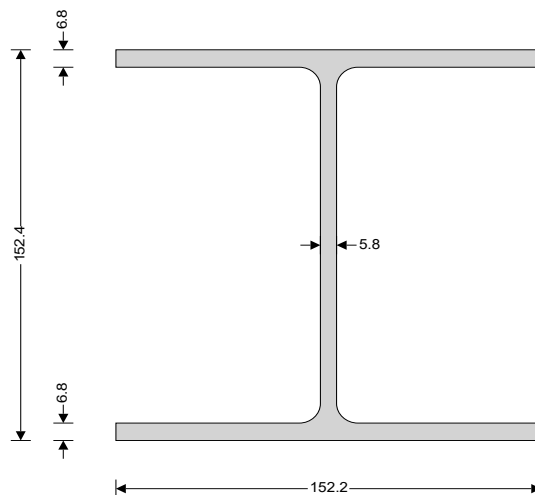
$\max(T, t) = 6.8 \text{ mm}$

Design strength

$p_y = 275 \text{ N/mm}^2$

Modulus of elasticity

$E = 205000 \text{ N/mm}^2$

**Lateral restraint**

Span 1 has lateral restraint at supports only

Effective length factors

Effective length factor in major axis

$K_x = 1.00$

Effective length factor in minor axis

$K_y = 1.00$

Effective length factor for lateral-torsional buckling

$K_{LT,A} = 1.00 + 2 \times D$

$K_{LT,B} = 1.00 + 2 \times D$

Classification of cross sections - Section 3.5

$\varepsilon = \sqrt{[275 \text{ N/mm}^2 / p_y]} = 1.00$

ANALYSIS & DESIGN

BEAM B3

Internal compression parts - Table 11

Depth of section	$d = 123.6 \text{ mm}$	
	$d / t = 21.3 \times \varepsilon \leq 80 \times \varepsilon$	Class 1 plastic

Outstand flanges - Table 11

Width of section	$b = B / 2 = 76.1 \text{ mm}$	
	$b / T = 11.2 \times \varepsilon \leq 15 \times \varepsilon$	Class 3 semi-
compact		

Section is class 3 semi-compact

Shear capacity - Section 4.2.3

Design shear force	$F_v = \max(\text{abs}(V_{\max}), \text{abs}(V_{\min})) = 21.8 \text{ kN}$
	$d / t < 70 \times \varepsilon$
	Web does not need to be checked for shear buckling
Shear area	$A_v = t \times D = 884 \text{ mm}^2$
Design shear resistance	$P_v = 0.6 \times p_y \times A_v = 145.8 \text{ kN}$
	PASS - Design shear resistance exceeds design shear force

Moment capacity - Section 4.2.5

Design bending moment	$M = \max(\text{abs}(M_{s1_max}), \text{abs}(M_{s1_min})) = 26.6 \text{ kNm}$
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Effective plastic modulus - Section 3.5.6

Limiting value for class 2 compact flange	$\beta_{2f} = 10 \times \varepsilon = 10$
Limiting value for class 3 semi-compact flange	$\beta_{3f} = 15 \times \varepsilon = 15$
Limiting value for class 2 compact web	$\beta_{2w} = 100 \times \varepsilon = 100$
Limiting value for class 3 semi-compact web	$\beta_{3w} = 120 \times \varepsilon = 120$
Effective plastic modulus - cl.3.5.6.2	
	$S_{\text{eff}} = \min(Z_{xx} + (S_{xx} - Z_{xx}) \times \min(\frac{((\beta_{3w} / (d / t))^2 - 1)}{((\beta_{3w} / \beta_{2w})^2 - 1)}, \frac{((\beta_{3f} / (b / T) - 1)}{(\beta_{3f} / \beta_{2f} - 1)})), S_{xx}) = 176245 \text{ mm}^3$

Moment capacity low shear - cl.4.2.5.2	$M_c = \min(p_y \times S_{\text{eff}}, 1.2 \times p_y \times Z_{xx}) = 48.5 \text{ kNm}$
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Effective length for lateral-torsional buckling - Section 4.3.5

Effective length for lateral torsional buckling	$L_E = 1.0 \times L_{s1} + 2 \times D = 5305 \text{ mm}$
Slenderness ratio	$\lambda = L_E / r_{yy} = 143.454$

Equivalent slenderness - Section 4.3.6.7

Buckling parameter	$u = 0.840$
Torsional index	$x = 20.701$
Slenderness factor	$v = 1 / [1 + 0.05 \times (\lambda / x)^2]^{0.25} = 0.736$
Ratio - cl.4.3.6.9	$\beta_w = S_{\text{eff}} / S_{xx} = 0.968$
Equivalent slenderness - cl.4.3.6.7	$\lambda_{LT} = u \times v \times \lambda \times \sqrt{\beta_w} = 87.277$
Limiting slenderness - Annex B.2.2	$\lambda_{L0} = 0.4 \times (\pi^2 \times E / p_y)^{0.5} = 34.310$

$\lambda_{LT} > \lambda_{L0}$ - Allowance should be made for lateral-torsional buckling

Bending strength - Section 4.3.6.5

Robertson constant	$\alpha_{LT} = 7.0$
Perry factor	$\eta_{LT} = \max(\alpha_{LT} \times (\lambda_{LT} - \lambda_{L0}) / 1000, 0) = 0.371$
Euler stress	$p_E = \pi^2 \times E / \lambda_{LT}^2 = 265.6 \text{ N/mm}^2$
	$\phi_{LT} = (p_y + (\eta_{LT} + 1) \times p_E) / 2 = 319.5 \text{ N/mm}^2$
Bending strength - Annex B.2.1	$p_b = p_E \times p_y / (\phi_{LT} + (\phi_{LT}^2 - p_E \times p_y)^{0.5}) = 149.1 \text{ N/mm}^2$

Equivalent uniform moment factor - Section 4.3.6.6Moment at quarter point of segment $M_2 = 20.5$ kNmMoment at centre-line of segment $M_3 = 26.6$ kNmMoment at three quarter point of segment $M_4 = 19.7$ kNmMaximum moment in segment $M_{abs} = 26.6$ kNmMaximum moment governing buckling resistance $M_{LT} = M_{abs} = 26.6$ kNm

Equivalent uniform moment factor for lateral-torsional buckling

$$m_{LT} = \max(0.2 + (0.15 \times M_2 + 0.5 \times M_3 + 0.15 \times M_4) / M_{abs}, 0.44) = 0.927$$

Buckling resistance moment - Section 4.3.6.4Buckling resistance moment $M_b = p_b \times S_{eff} = 26.3$ kNm

$$M_b / m_{LT} = 28.3 \text{ kNm}$$

PASS - Buckling resistance moment exceeds design bending moment**Check vertical deflection - Section 2.5.2**

Consider deflection due to dead, imposed and other loads

Limiting deflection $\delta_{lim} = L_{s1} / 250 = 20$ mmMaximum deflection span 1 $\delta = \max(\text{abs}(\delta_{max}), \text{abs}(\delta_{min})) = 17.905$ mm***PASS - Maximum deflection does not exceed deflection limit***